

# Circles, Arcs, Sectors & Radians Practice Questions

DO NOT USE A CALCULATOR ON ANY OF THE FOLLOWING QUESTIONS UNLESS INDICATED.

- What is the area, in units squared, of a circle with radius of 11 units?
  - $\frac{11}{2}\pi$
  - $11\pi$
  - $22\pi$
  - $121\pi$
- What is the circumference, in units, of a circle with radius of 20 units?
  - $10\pi$
  - $20\pi$
  - $40\pi$
  - $400\pi$
- What is the radius, in inches, of a circle with circumference of  $64\pi$  inches?
  - 8
  - 16
  - 32
  - 64
- What is the radius, in centimeters, of a circle with area of  $100\pi$  centimeters squared?
  - 10
  - 25
  - 50
  - 200
- FREE RESPONSE: What is the measure, in degrees, of an angle with measure  $\frac{2\pi}{3}$  radians?
- FREE RESPONSE: What fraction of a circle is represented by an arc of  $100^\circ$ ?
- What fraction of a circle is represented by an arc angle of  $\frac{4\pi}{9}$  radians?
  - $\frac{1}{9}$
  - $\frac{2}{9}$
  - $\frac{4}{9}$
  - $\frac{8}{9}$

8. What is the sector area, in square units, of a sector representing  $\frac{3}{5}$  of a circle with radius 10 units?

- (A)  $8\pi$
- (B)  $12\pi$
- (C)  $40\pi$
- (D)  $60\pi$

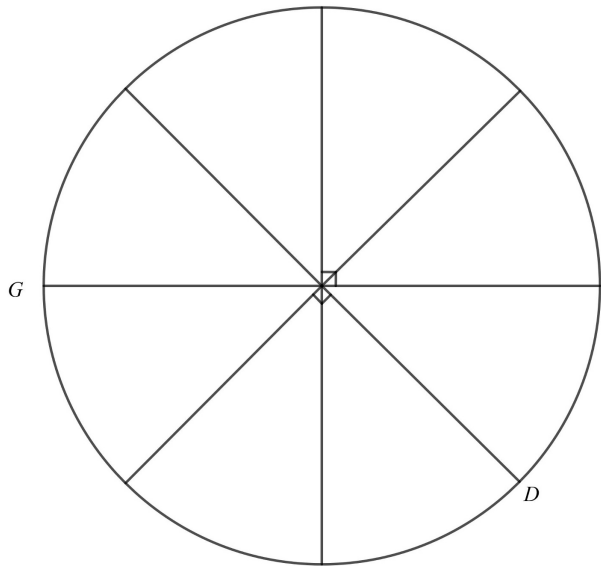
9. (CALCULATOR) Circle  $C$  has a radius of 6 inches. What is the sector area, in square inches, of a sector of Circle  $C$  with an arc angle of  $200^\circ$ ?

- (A)  $4\pi$
- (B)  $\frac{20}{3}\pi$
- (C)  $16\pi$
- (D)  $20\pi$

10. What is the arc length, in centimeters, of an arc with angle measure  $\frac{3\pi}{4}$  radians in a circle of radius 10 centimeters?

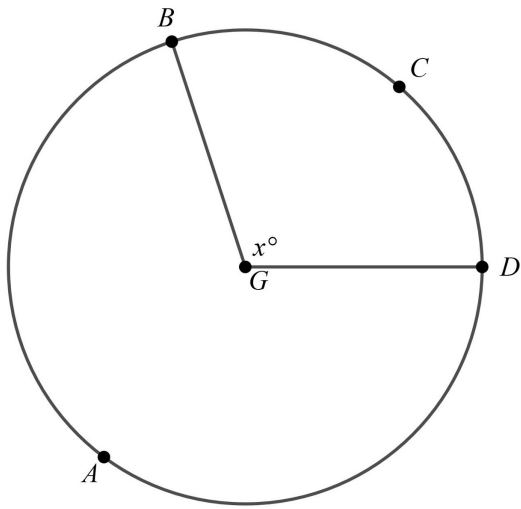
- (A)  $\frac{\pi}{4}$
- (B)  $\frac{15}{2}\pi$
- (C)  $15\pi$
- (D)  $75\pi$

11. (CALCULATOR) FREE RESPONSE: The number of radians in a 1080-degree angle can be written as  $n\pi$ , where  $n$  is a constant. What is the value of  $n$ ?



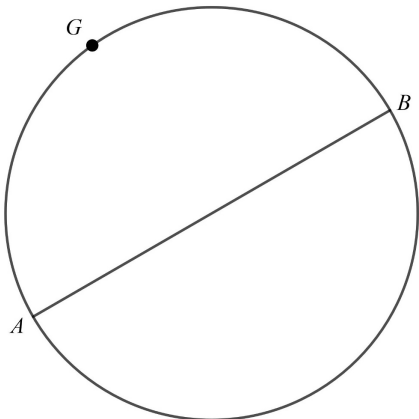
12. The circle above has a circumference of 48. What is the length of minor arc  $DG$ ?

- (A) 6
- (B) 12
- (C) 18
- (D) 48



13. (CALCULATOR) The circle above has center  $G$ , the length of arc  $BCD$  is  $9\pi$  and  $x = 108$ . What is the length of major arc  $BAD$ ?

- (A)  $18\pi$
- (B)  $21\pi$
- (C)  $27\pi$
- (D)  $30\pi$

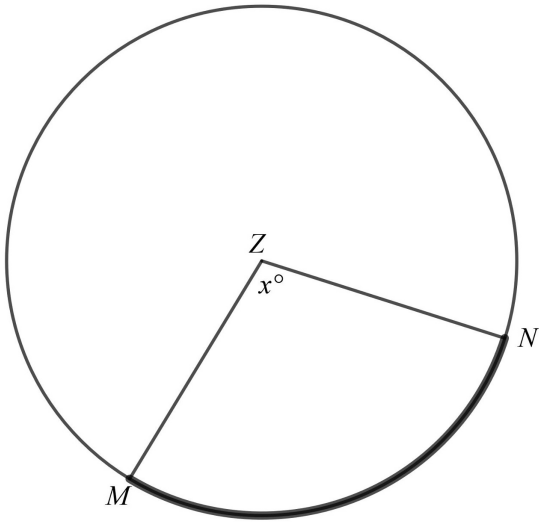


14. In the circle above, segment  $AB$  is a diameter. If the length of arc  $AGB$  is  $3\pi$ , what is the length of the radius of the circle?

- (A) 1.5
- (B)  $\sqrt{6}$
- (C) 3
- (D) 6

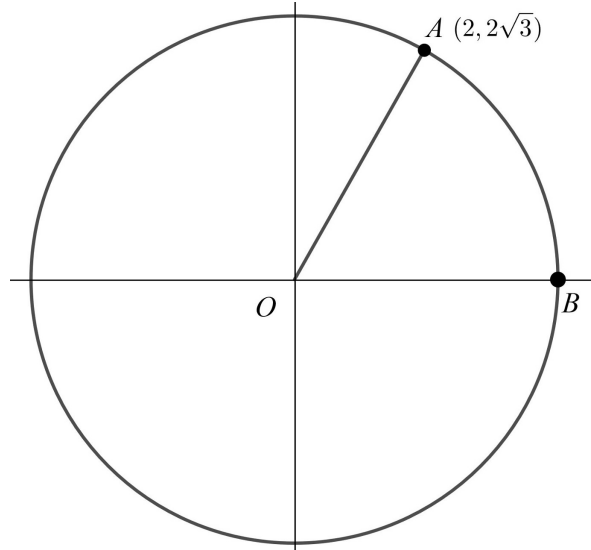
15. FREE RESPONSE: In a circle with center  $P$ , central angle  $APB$  has a measure of  $\frac{7}{4}\pi$  radians. The area of the sector formed by central angle  $APB$  is what fraction of the area of the circle?

16. FREE RESPONSE: Points  $X$  and  $Y$  lie on a circle with radius 0.5, and arc  $XY$  has length  $\frac{3\pi}{8}$ . What fraction of the circumference of the circle is the length of arc  $XY$ ?

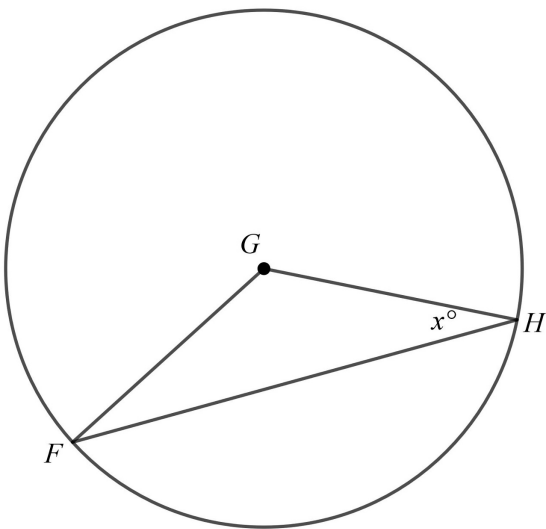


Note: Figure not drawn to scale.

17. (CALCULATOR): In the figure above, the circle has center  $Z$  and radius 9. If the length of arc  $MN$  (shown in bold) is between 2 and 3, what is one possible integer value of  $x$ ?



19. FREE RESPONSE: In the  $xy$ -plane above,  $O$  is the center of the circle and the measure of angle  $\angle AOB$  is  $\frac{\pi}{n}$  radians. What is the value of  $n$ ?



Note: Figure not drawn to scale.

18. (CALCULATOR) FREE RESPONSE: In the circle above, point  $G$  is the center and the length of minor arc  $FH$  is  $\frac{4}{9}$  of the circumference of the circle. What is the value of  $x$ ?

20. (CALCULATOR) FREE RESPONSE: In Circle  $A$  with centerpoint  $K$ , the length of minor arc  $RS$  is  $4\pi$  with an arc angle of  $\frac{2\pi}{5}$  radians. If the area of major sector  $RS$  is  $n\pi$  square units, what is the value of  $n$ ?

# Equation of a Circle, Completing the Square & Distance Formula Practice Questions

YOU MAY USE A CALCULATOR ON THE FOLLOWING QUESTIONS.

1. A circle in the  $xy$ -plane has center  $(1,3)$  and radius  $4$ . Which of the following is an equation of the circle?

- (A)  $(x-1)^2 + (y-3)^2 = 4$
- (B)  $(x+1)^2 + (y+3)^2 = 4$
- (C)  $(x-1)^2 + (y-3)^2 = 16$
- (D)  $(x+1)^2 + (y+3)^2 = 16$

2. A circle in the  $xy$ -plane has center  $(4,-6)$  and radius  $3$ . Which of the following is an equation of the circle?

- (A)  $(x+4)^2 + (y-6)^2 = 3$
- (B)  $(x-4)^2 + (y+6)^2 = 3$
- (C)  $(x-4)^2 + (y+6)^2 = 9$
- (D)  $(x+4)^2 + (y-6)^2 = 9$

$$(x-2)^2 + (y+5)^2 = 25$$

3. In the  $xy$ -plane, the graph of the equation above is a circle. Point  $G$  is on the circle and has coordinates  $(7,-5)$ . If  $\overline{FG}$  is a diameter of the circle, what are the coordinates of point  $F$ ?

- (A)  $(-3,-5)$
- (B)  $(2,5)$
- (C)  $(5,0)$
- (D)  $(5,-10)$

4. A circle in the  $xy$ -plane has equation  $(x-4)^2 + (y+3)^2 = 36$ . Which of the following points does NOT lie in the interior of the circle?

- (A)  $(-1,-5)$
- (B)  $(-2,0)$
- (C)  $(0,0)$
- (D)  $(8,-5)$

5. In the  $xy$ -plane, the graph of  $x^2 + y^2 - 6x + 2y = -1$  is a circle. What is the radius of the circle?
- (A) 1  
 (B) 3  
 (C)  $2\sqrt{3}$   
 (D) 9
6. Which of the following is an equation of a circle in the  $xy$ -plane with center  $(-2, 3)$  and a radius with endpoint  $(5, 1)$ ?
- (A)  $(x + 2)^2 + (y - 3)^2 = 53$   
 (B)  $(x - 2)^2 + (y + 3)^2 = 53$   
 (C)  $(x - 2)^2 + (y + 3)^2 = \sqrt{53}$   
 (D)  $(x + 2)^2 + (y - 3)^2 = \sqrt{53}$
7. In the  $xy$ -plane, the graph of  $3x^2 + 18x + 3y^2 + 12y = 9$  is a circle. What is the centerpoint of the circle?
- (A)  $(3, 2)$   
 (B)  $(6, 4)$   
 (C)  $(-6, -4)$   
 (D)  $(-3, -2)$
8. Which of the following is an equation of a circle in the  $xy$ -plane with center  $(-5, 6)$  and a radius with endpoint  $(2, -7)$ ?
- (A)  $(x - 5)^2 + (y + 6)^2 = \sqrt{218}$   
 (B)  $(x + 5)^2 + (y - 6)^2 = \sqrt{218}$   
 (C)  $(x - 5)^2 + (y + 6)^2 = 218$   
 (D)  $(x + 5)^2 + (y - 6)^2 = 218$
9. In the  $xy$ -plane, the graph of  $2x^2 + 14x + 2y^2 - 8y = 17.5$  is a circle. What is the centerpoint of the circle?
- (A)  $(-7, -4)$   
 (B)  $(-3.5, 2)$   
 (C)  $(3.5, -2)$   
 (D)  $(5, 5)$
10. In the  $xy$ -plane, the graph of  $2x^2 + 6x + 2y^2 - 10y = 1$  is a circle. What is the radius of the circle?
- (A)  $\sqrt{3}$   
 (B)  $3\sqrt{3}$   
 (C) 3  
 (D) 9